# Augmented Reality Based on Estimation of Defocusing and Motion Blurring from Captured Images

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### ABSTRACT

Photometric registration is as important as geometric registration to generate a seamless augmented reality scene. Especially the difference in image quality between a real image and virtual objects caused by defocusing and motion blurring in capturing a real scene image easily exhibits the seam between real and virtual worlds. To avoid this problem in video see-through augmented reality, it is necessary to simulate the optical system of camera when virtual objects are rendered. This paper proposes an image composition method for video see-through augmented reality, which is based on defocusing and motion blurring estimation from the captured real image and rendering of virtual objects with blur effects. In experiments, the effectiveness of the proposed method is confirmed by comparing a real image with virtual objects rendered by the proposed method.

**CR Categories:** H.5.1 [Information interfaces and presentation]: Multimedia Information Systems—Artificial, augmented, and virtual realities

**Keywords:** augmented reality, photometric registration, blur estimation, point spread function, image quality

# **1** INTRODUCTION

Augmented reality is a technology which provides users with location-based information by overlaying virtual objects on the real world[1, 2]. In augmented reality, it is important to resolve some registration problems including geometric and photometric registration problems. The geometric registration means that the position and the orientation of virtual objects are consistent with the real world under varying viewpoints. The photometric registration means that shadow and shading of virtual objects and their image quality are consistent with the real world.

Recently, there are a number of researches that are intended to increase the photometric consistency[3, 4, 5]. However, they have concentrated mainly on shadow and shading of virtual objects and there are few attempts focused on the quality of virtual objects in the composed image. Especially, in video see-through augmented reality, the seamlessness of the real and virtual worlds is affected by the differences in image quality between superimposed virtual objects and the real image. This problem is caused by the difference between real and virtual camera models. In general, an ideal camera model which means that the image quality is not degraded by the lens is used when rendering virtual objects. However, there is deterioration in an image captured by a real camera. Some attempts have been done to reduce the difference between real and virtual worlds, which change the image quality of real image and rendered virtual objects with "cartoon-like" or "sketch-like" representation[6, 7].

In order to resolve the real and virtual camera model inconsistency, it is necessary to estimate the deterioration of captured image and to represent the blur effect on virtual objects. In image processing and computer vision, image restoration methods based on estimation of image degradation described by the point spread function (PSF) have been proposed[8]. However, these techniques need much calculation cost because most of them are based on iterative computation. Thus such techniques are not suitable for augmented reality which requires real time operation. On the other hand, in computer graphics, there are some researches which achieve realistic rendering of virtual objects simulating the real camera[9, 10]. However, it is also difficult for these techniques to apply to augmented reality because lens parameters, which are changed by lens operations, always need to be known and intrinsic camera parameters should be calibrated in advance in the related work.

To realize consistent image quality in augmented reality, this paper copes with both defocusing and motion blurring caused by the camera, that are typical factors of the deterioration of image. We propose a technique which equalizes the quality of the real image captured by the real camera and the rendered virtual objects. The proposed method merges a captured image and rendered virtual objects with blur effects estimated from a real scene image containing a marker. We also propose an improved geometric registration method which can detect the image marker accurately by eliminating the blur effect from the captured image by using the estimated blur parameters.

This paper is structured as follows. Section 2 briefly reviews related work. Section 3 describes a blur model of image, a blur estimation method, and a method for estimating the camera position and orientation from an image marker. A method of rendering virtual objects based on reproduction of estimated blur is explained as well. In Section 4 experimental results are described. Finally, Section 5 gives conclusion and future work.

# 2 RELATED WORK

Estimation of image degradation has been studied in computer vision. In computer graphics, some techniques which can render virtual objects with blur effects have been proposed.

Estimations of blur from images: In computer vision, in order to restore the degraded image, most methods estimate the PSF which models the degradation of image and recover the image by removing the effects of the PSF. In general, these methods can be divided into two approaches according to assumptions. One estimates the blur effect based on analyzing patterns on a target object as knowledge. The other does not have any knowledge about the target objects. One of the former approaches is an estimation of the PSF of a scanner[11]. This technique can estimate the scanner property described by the PSF scanning known patterns. The latter approach is called blind deconvolution, which attempts to recover target objects from a set of blurred images. There are a number of techniques which treat the same problem. The depth from defocusing[12, 13, 14] and the super-resolution[15, 16, 17] are typ-

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ical techniques, which also estimate the PSF simultaneously.

Blur representation on virtual objects: In computer graphics, there are a number of techniques to reproduce various effects caused by a camera. These techniques contribute to render virtual objects realistically. For example, Nakamae et al.[18] have proposed a photo montage technique for landscape environment assessment. This technique can improve the quality of final montage image with consideration of the seamlessness of the border between a photograph and superimposed virtual objects. Furthermore, there are a number of researches to generate more realistic effects caused by a real camera assuming lens model of the camera. For example, Kolb et al.[9] have proposed a rendering technique simulating an optical system of real camera. This method can reproduce the depth of focus effect which is characterized by the design of lens. Asada and Baba[10] have proposed a rendering technique with a new camera model which has zoom, focus and iris parameters. Their method can treat the relation among lens parameters systematically and achieve rendering of virtual objects with the depth of field effect in real time.

The proposed method in this paper combines blur estimation in computer vision with blur representation in computer graphics. Note that most of PSF estimation methods in computer vision are aimed at arbitrary PSFs. These methods take much calculation cost and thus it is difficult to apply such methods for augmented reality which requires real time processing. In the proposed method, in order to achieve the real time processing, the PSF which represents both defocusing and motion blurring is modeled approximately and the parameter of PSF is estimated by using an image marker whose color and shape are known. On the other hand, in computer graphics, most techniques for rendering blur effects assume off-line processing. In addition, many parameters changed by lens operations of the camera are required to simulate blur effects. In the proposed method, the blur effect is represented by applying a simple filter determined by the PSF to rendered virtual objects. Moreover, the calculation cost of this processing is reduced by using graphics hardware acceleration.

#### **3** AUGMENTED REALITY BASED ON BLUR ESTIMATION

The proposed method reduces the difference in image quality between the real and virtual objects in augmented reality by estimating the PSF from an observed image marker in a real scene, and reproducing the PSF to virtual objects. We use pixel intensities around the edge of image marker to estimate the PSF. When the image is blurred, the intensity changes gradually along the direction orthogonal to the edge. In this paper, the change in intensity profile on the edge is described as the width of blur. The shape of PSF is estimated by integrating the width of blur in edges in various directions.

In some augmented reality systems, virtual objects are composed around image markers in the real world[19]. In this case, we can assume that the blur effect on virtual objects is represented by the degree of blur at the marker because the PSF is related to the depth of the target object and the change of depth is not large around the marker in most case.

Fig. 1 illustrates a flow diagram of the proposed method. First, the real scene is captured by a camera, and image markers whose color and shape are known are detected (Fig. 1 (A)). In the second step, the width of blur is estimated by fitting a function defined by a model of PSF to intensities in an edge region of the marker, and the parameters of PSF are acquired by integrating the estimated width of blur in various directions (Fig. 1 (B)). Next, the camera position and orientation in marker coordinate system are estimated by recovering the shape of the marker using the estimated blur parameters (Fig. 1 (C)). Finally, virtual objects are rendered with the blur effect and are composed with the real image (Fig. 1 (D)). The blur



Figure 1: Flow diagram of the proposed method.



f: focal length of the lens v: distance from the lens to the image plane w: depth from the lens to the object

Figure 2: Defocusing caused by the lens.

model of a camera and the image marker as well as processes (A) to (D) are explained in the following sections.

#### 3.1 Model of defocusing and motion blurring

In general, the blur effect caused by the camera includes two major factors: defocusing and motion blurring. The blurred image is generated by convolution of an ideal image with the PSF which expresses effects of defocusing and motion blurring. The blur caused by defocusing depends on depth from the center of lens to an object, the aperture of lens, and the resolution of camera. The blur of image is caused by defocusing of lens as shown in Fig. 2. Note that the radius r of an optical disk on the image plane is defined by Eq. (1), and r depends on the position in the image[20].

$$r = \rho \gamma v \left| \frac{1}{f} - \frac{1}{v} - \frac{1}{w} \right|, \qquad (1)$$

where f, w and v mean the focal length of lens, the depth from lens to an object and the distance from lens to the image plane, respectively.  $\gamma$  and  $\rho$  mean the aperture of lens and a constant which depends on the resolution of CCD, respectively.

In general, two dimensional circular spread of light is used as a kernel of PSF (pill-box) of defocusing. In addition, the radius rof optical disk depends on the position in the image. In this paper, the PSF is assumed to be a function which does not depend on the position in the image[21], since virtual objects are placed around a marker in the captured image; that is, we assume that the radius of optical disk r is constant around the marker. The PSF of blur caused by defocusing of camera is defined as follows:

$$R(x,y;r) = \begin{cases} \frac{1}{\pi r^2} & ; & \text{where } x^2 + y^2 \le r^2 \\ 0 & ; & \text{otherwise} \end{cases}, \quad (2)$$

where x and y represent the position of target pixel, and r shows the radius of the PSF which is equivalent to the radius of optical disk. In this paper, r is considered as the parameter of blur caused by defocusing.

The motion blurring depends on the motion of camera, movement of target object and the exposure of camera. The motion of camera and the movement of target object are generally very complicated, and so the formulation of the PSF is very complex. In this paper, we assume that the motion of camera and the movement of target object can be represented by one-dimensional translation in the image plane of camera. The PSF of motion blurring is now again as follows:

$$L(x,y;l,\theta) = \frac{1}{2l} \left( u(x'+l) - u(y'-l) \right) \delta(y'), \quad (3)$$

where

$$\begin{pmatrix} x'\\ y' \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta\\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} x\\ y \end{pmatrix}.$$
 (4)

Note that *x* and *y* represent the position of target pixel. The function u(x) shows the unit step function and  $\delta(t)$  denotes the Dirac's delta function. *l* and  $\theta$  mean the length of uniform motion and the direction of motion, respectively. Note that *l* and  $\theta$  are considered as parameters of blur effect by motion blurring.

This paper treats the blur effect caused by both defocus and camera motion. The model of PSF is obtained by convoluting Eq. (2) with Eq. (3). However, the calculation cost of convolution required in estimation of the PSF parameters is not small, thus it is not acceptable for augmented reality. In order to achieve the real time processing, we simplify the PSF. In the proposed method, the following approximated PSF is employed.

$$P(x,y;r,l,\theta) = \begin{cases} \frac{1}{\pi((r+l)^2 + r^2)} & ; \quad \left(\frac{x'}{r+l}\right)^2 + \left(\frac{y'}{r}\right)^2 \le 1 \\ 0 & ; \quad \text{otherwise} \end{cases}$$
(5)

where

$$\begin{pmatrix} x'\\ y' \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta\\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} x\\ y \end{pmatrix}.$$
(6)

Here, *x* and *y* represent the position of target pixel in the image. *r*, *l* and  $\theta$  show the radius of defocusing blur, the length of uniform motion and the direction of motion, respectively. In this paper, *r*, *l* and  $\theta$  are considered as parameters of the PSF of blur. The above equation means an elliptical spread of light on an image plane. The direction of major axis of the ellipse shows the motion direction of camera. From this approximation of PSF, the profile of blurred edge can be described by a formula, so that calculation cost of estimating the PSF parameters can be reduced.

#### 3.2 Image marker

A square marker with known shape and color is used to estimate the camera position and orientation[19]. Fig. 3 illustrates the pattern of the marker used in this study. The edge of inner circle in the marker is used to estimate the parameters of PSF. The role of each part of the marker is as follows.

- (a) **ID area:** This area is used to identify the marker by recognizing the pattern of black circle.
- (b) Circular edge: This edge is used to estimate parameters of PSF. The proposed method acquires the PSF from the parameters estimated at multiple points on the edge in various directions.
- (c) **Corners of square marker:** These corners are used to determine the camera position and orientation in the marker coordinate system for geometric registration.



#### 3.3 Detection of marker from captured image: Process (A)

Marker of known shape and color is detected by the following standard processes.

- 1. **Extraction of marker region:** An image captured by camera is binarized and is labeled. Regions whose size is large enough are detected as candidates of marker.
- 2. **Detection of marker corners:** Each edge of the marker is detected by fitting a straight line. Corners of marker are then determined by calculating intersections of detected lines.

Note that the position of corner of marker may include some errors caused by the blur effect. When a threshold is not suitable in the binarization process, the marker will be shrunk or expanded because the intensity of blurred edge changes gradually. Since the camera position and orientation are estimated by solving the PnP problem (n = 4)[19], the accuracy of position and orientation of camera is affected by the accuracy of detected corner positions in the image. In this paper, this problem is resolved by eliminating the blur effect in process (C) described in Section 3.6.

#### 3.4 Estimation of width of blur: Process (B)

The width of blur is estimated in various directions at multiple points on the circular edge of marker before estimating parameters of PSF. This section explains estimation of the width of blur from change of intensity along the direction orthogonal to the edge.

Provided that an ideal edge profile of marker is expressed by the step function shown in Fig. 4(a), the intensity of edge affected by the blur effect expressed by the PSF[13] is given as follows:

$$f(\vec{p}; d, \vec{p}_0, i_{min}, i_{max}) = \begin{cases} i_{min} & ; t < -1 \\ g(t)(i_{max} - i_{min}) + i_{min} & ; -1 \le t \le 1 \\ i_{max} & ; t > 1 \end{cases}$$
(7)

where

t

$$\dot{t} = \frac{(\vec{p} - \vec{p}_0) \cdot \vec{o}}{d}, \tag{8}$$

$$g(t) = \frac{1}{2} + \frac{1}{\pi} \left( t \sqrt{1 - t^2} + \arcsin t \right),$$
 (9)

and  $\vec{o}$  is the normalized direction orthogonal to the edge.  $\vec{p}$  and  $\vec{p}_0$  are the position of pixel and the position of edge which is not affected by the blur effect, respectively. The parameter *d* means the width of blur which is equivalent to the width of slope of the intensity along the direction orthogonal to the edge.  $i_{min}$  and  $i_{max}$  show the minimum and maximum values of intensities of the edge. Parameters of blur are estimated by fitting a function shown in Eq. (7) to the edge profile in the image. Fig. 4(a) illustrates the profiles of ideal and blurred edges. Parameters  $d, \vec{p}_0, i_{min}$  and  $i_{max}$  are



Figure 4: Function fitting to blurred edge and sampled pixels used in blur estimation.

estimated by minimizing the error defined by Eq. (10) using the quasi-Newton method.

$$E_{edge}(d, \vec{p}_0, i_{min}, i_{max}) = \sum_{i=1}^{N} \{I(\vec{p}_i) - f(\vec{p}_i; d, \vec{p}_0, i_{min}, i_{max})\}^2.$$
(10)

In Eq. (10),  $\vec{p}_i$ ,  $I(\vec{p}_i)$  and *N* mean the position of the *i*-th pixel, the intensity of the pixel along the direction orthogonal to the edge and the number of sampled pixels, respectively. Lines in Fig. 4(b) indicate pixels used for blur estimation. The position of circular edge in the image marker is determined from a marker region detected in process (A) described in Section 3.3.

# 3.5 Estimation of PSF parameters: Process (B)

The blur sizes estimated at multiple points on the edge of circle are integrated to determine parameters of the PSF. Note that the kernel of PSF has an elliptical shape and the eccentricity of the ellipse is the same as the estimated width of blur. The parameters r, l and  $\theta$  of the PSF are estimated by minimizing the error function defined by Eq. (11) using the quasi-Newton method.

$$E_{PSF}(r,l,\theta) = \sum_{j=1}^{M} \frac{\left\{ d_j - h(\theta_j;r,l,\theta) \right\}^2}{E_{edge,j}}, \quad (11)$$

where

$$h(\theta_{j};r,l,\theta) = \frac{1}{\sqrt{\left(\frac{\cos(\theta_{j}-\theta)}{r+l}\right)^{2} + \left(\frac{\sin(\theta_{j}-\theta)}{r}\right)^{2}}}, \quad (12)$$

and *j* represents the index of edge. *r*, *l* and  $\theta$  mean parameters of the PSF described in Section 3.1.  $h(\theta_j; r, l, \theta)$  represents the eccentricity of the ellipse about the direction  $\theta$ .  $d_j$  and  $E_{edge,j}$  denote the width of blur estimated from *j*-th point on edge and the error in the estimation mentioned in Section 3.4, respectively.

# **3.6** Estimation of camera position and orientation in consideration of blur effects: Process (C)

In order to estimate the camera position and orientation accurately, it is necessary to recover the shape of marker by removing the influence of blur. There are two approaches to recover the marker shape. One is an image processing method based on inverse filtering. The marker is restored by applying the inverse filter to the image degraded by blur effects. The other is a restoration method using geometrical features used to estimate the edge of marker. In this paper, to achieve a real time processing required by the augmented reality, the latter based on the estimation of edge position is applied. Corners of marker are detected from intersections of lines which represent edges of the marker. The camera position and orientation are estimated from positions of corners of the marker in the image. The detail of processing is as follows.

- 1. The process described in Section 3.4 is applied to outer edges of the marker since this process can estimate the accurate edge position  $\vec{p}_0$  under blur effect.
- 2. The lines of outer edge of the marker are estimated by fitting lines to edge positions.
- 3. Four corners of the square marker are determined from intersections of lines, and the camera position and orientation in the marker coordinate system are then computed by solving the PnP problem (n = 4).

Note that the camera position and orientation can be more accurate than those estimated by standard techniques such as [19] because the positions of corners estimated by this process are not influenced by the blur effects.

## 3.7 Rendering of virtual objects with blur effects: Process (D)

In order to achieve real time computation, the processes of rendering and simulation of blur effects are computed using graphics hardware. First, virtual objects are rendered to a texture buffer with the camera position and orientation estimated in Section 3.6. Then, a smoothing filter with the estimated PSF is applied to the rendering result. The kernel of PSF is the same as Eq. (5). Here, only a neighborhood of  $4(r+l)^2$  pixels is calculated to accelerate the computation. Furthermore, the branching function of OpenGL shading language is used so that pixels outside of the PSF are excluded.

#### 4 EXPERIMENTS

In experiments, in order to confirm that the proposed method can decrease the difference in image quality between the real image and virtual objects, we have compared the real image with a virtual object rendered by the proposed method. Experiments are carried out using a desktop PC (CPU : PentiumD 3.0GHz, Memory : 3.25GByte, Graphics card : Radeon X1900XTX) and a USB camera (ARGO Lu-135c, Resolution :  $1024 \times 768$  pixels, Capturing frame rate: 15fps). Square markers are placed in the real world and a virtual object is composed by recognizing the markers. Moreover, the graphics hardware is used when the filtering process of blur effects is applied to virtual objects as mentioned in the previous section. First, we confirm the accuracy of parameters of PSF estimated by the proposed method described in Sections 3.4 and 3.5.

# 4.1 Evaluation of camera position estimation using blur parameters

In this section, in order to verify the accuracy of camera position estimation using blur parameters, we have carried out a quantitative evaluation. The estimated distance from camera to marker is investigated under varying the focus of camera and fixing the positions of camera and marker. Here, the distance from camera to marker is set to 900mm.

Fig. 5 shows the relationship between the estimated width of blur and the estimated camera position when the focus of camera changes. Figs. 5 (a) and (b) are cases when the focus is changed to near and far, respectively. They also illustrate selected 250 samples under various focus values. From these results, we can confirm that the distance from camera to marker by the conventional method[19] increases when the size of defocusing is large. This is become the region of marker is detected by a simple binarization method with



Figure 5: Estimated distance from camera to marker under change of focus of camera.

a threshold and thus extracted region is smaller than the actual size of the marker. On the other hand, it is clearly shown in Fig. 5 that the distance is estimated accurately by the proposed method even if the width of blur is large.

### 4.2 Evaluation of estimated parameters of PSF in simulation

To verify the accuracy of parameters of PSF, we have carried out a quantitative evaluation of estimated parameters in simulation. Images used in this experiment are generated with various blur values. The parameter of defocusing r is changed by 0.5 from 0.5 to 4.5. Parameters of motion blurring l and  $\theta$  are changed by 0.5 from 0 to 4.5 and by  $\pi/8$  from 0 to  $\pi$ , respectively. In this evaluation, we have computed the difference between ground truth and the estimated parameters. The difference larger than zero means that the estimated parameter of blur is larger than the simulated parameter.

Fig. 6 illustrates the relationship between the simulation and estimated parameters. In Fig. 6(a), each sequence shows the variation of the parameter r for different values of parameter l. Except for the case where parameter r is 0.5, the difference of parameter rbetween the simulation and estimated parameter is about 0.5. Fig. 6(b) shows the difference of the parameter *l*. Each sequence shows the variation of the parameter l for different values of parameter r. The difference of parameter l between the simulation and estimated parameter is about -0.5 excepting the case where parameter r is 0.5. In addition, the difference of the parameter  $\theta$  between the simulation and estimated parameter is from -0.24 to 0.24 radians. Here, estimated parameters of PSF include errors because the estimation of width of blur becomes unstable when the parameter r is smaller than 1. However, we consider that the estimated parameters of PSF are almost accurate in order to reproduce both defocusing and motion blurring.

#### 4.3 Comparison between real and virtual objects in augmented scene image

To confirm the effectiveness of the proposed method, rendered virtual objects are compared with a real image fixing and changing the



(a) The difference in the size of defocusing (r).



(b) The difference in the size of motion blurring (l).

Figure 6: Errors between estimated parameter and parameter used in simulation.

focus of camera. We compare real objects captured by the camera with composed virtual objects. Composed results of virtual objects by a conventional method which does not represent the blur of real image are also shown.

**Static scene with motion blurring:** Fig. 7 shows real and augmented scene images under motion blurring. Figs. 7(a), (b) and (c) show a captured image, an augmented image without consideration of motion blurring and an augmented image with consideration of motion blurring, respectively. We can see the difference between the real object and the virtual object in Fig. 7(b). For example, the pattern in the real cube circumscribed by (A) in Fig. 7(a) is affected by the blur effect and horizontal edges in the image are disappeared. However, edges of the virtual object circumscribed by (B) in Fig. 7(b), which is rendered without motion blurring estimation, exist distinctly. On the other hand, edges of the virtual object circumscribed by (C) in Fig. 7(c), which is rendered with motion blurring estimation, are disappeared and the appearance is similar to that of the real object.

**Static scene with different focus of camera:** Fig. 8 shows the experimental scene. A cylindrical real object is located at 150mm from the camera. The marker and the real object for evaluation are at 300mm from the camera. A checker board is placed at 900mm from the camera. The real object to be compared is a cube whose surfaces have grid patterns, and the same object is merged into a real image as a virtual object. When the virtual object is rendered, the light environment is manually tuned and the shadow was not rendered.

Fig. 9 shows augmented scene images with different focuses. Fig. 9(i) is focused on a near object, (ii) is focused on a marker, and (iii) is focused on a far object. In augmented scenes without blur estimation in column (a) of Fig.9, though a blur effect on the real object (right cube) is caused by defocusing, the virtual object (left cube) is composed without such an effect. Therefore, there can be observed the inconsistency of image quality between the real image and the virtual object and the seamlessness is not achieved. On the other hand, in column (b) of Fig. 9, the incompatibility caused by the difference in image quality has been reduced because the image quality of virtual object is matched with the real image. In the proposed method, the reproduced blur effect is uniform around the marker, although the difference in image quality is reduced. The



(a) Captured image (Camera motion is upward in the image.)

(b) Rendered image without motion blur estimation.

(c) Rendered image with motion blur estimation.

Figure 7: Results of merging a virtual object into a real scene image with motion blurring



Figure 8: Experimental environment

frame rate is approximately 15fps for rendering without blur estimation and 10fps for rendering with blur estimation. The frame rate is downed because the proposed method requires additional computational cost for estimating parameters of PSF and for applying blur effects on virtual objects.

# 5 CONCLUSION AND FUTURE WORK

This paper has proposed an image composition method which is based on estimation of blur from a real image for video see-through augmented reality. The proposed method can estimate parameters of approximated PSF by fitting a function to edges in a marker and by fitting an ellipse to the width of blur in various directions of the marker edge. We have also proposed a new method for estimating the camera position and orientation, which can eliminate the blur effect from the captured image. In experiments, have confirmed that the proposed method correctly estimates the parameters of PSF in simulation. Consequently, the method can seamlessly merge virtual objects into the real image which is affected by blur effects caused by defocusing and by motion blurring of camera. This has been proven through experiments.

In the present study, the approximated PSF has an elliptical shape and does not depend on the depth in the image. There are some limitations caused by this assumption. The virtual objects can be placed only around the marker, and PSFs of real cameras may not have an elliptical form. The following topics should further be investigated in future work.

- Consideration of arbitrary PSFs
- Calibration of intrinsic parameters of camera (*f*, *v*, *ρ* and *γ* shown in Section 3.1)

The former makes it possible to represent blur effects more accurately, and the latter makes it possible to apply blur effects on virtual objects not only around the marker but also at arbitrary positions.

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(i) Focused on a near object.



(ii) Focused on a marker.



(iii) Focused on a far object.

(a) Rendered without blur estimation.

(b) Rendered with blur estimation.

Figure 9: Results of merging a virtual object into a real scene image with defocusing. (Left column: rendering without blur estimation, right column: rendering with blur estimation. top row: focused on a near object, center row: focused on a marker, bottom row: focused on a far object.)

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